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**Title:** Cosmic particle acceleration by shocks and turbulence in merging galaxy clusters
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Characterizing the radio emission from the binary galaxy cluster merger Abell 2146

Abstract

The collisions of galaxy clusters generate shocks and turbulence in the intra-cluster medium (ICM). The presence of relativistic particles and magnetic fields is inferred through the detection of extended synchrotron radio sources, such as haloes and relics, and implies that merger shocks and turbulence are capable of (re-)accelerating particles to relativistic energies. However, the precise relationship between merger shocks, turbulence and extended radio emission is still unclear. Studies of the most simple binary cluster mergers are important to help understand the particle acceleration in the ICM. Our main aim is to study the properties of the extended radio emission and the particle acceleration mechanism(s) associated with the generation of relativistic particles in the ICM. We measure the low-frequency radio emission from the merging galaxy cluster Abell 2146 with LOFAR at 144 MHz. We characterize the spectral properties of the radio emission by combining these data with archival GMRT at 238, 612 MHz and VLA at 1.5 GHz data. Behind the NW and SE shocks we observe extended radio emission at 144 MHz. Across the NW extended source, the spectral index steepens from $-1.06 \pm 0.06$ to $-1.29 \pm 0.09$ in the direction of the cluster center. This spectral behavior suggests that a relic is associated with the NW upstream shock. The precise nature of the SE extended emission is unclear. It may be a radio halo bounded by a shock or a superposition of a relic and halo. At 144 MHz, we detect a faint emission which was not seen with high-frequency observations, implying a steep ($\alpha < -1.3$) spectrum nature of the bridge emission. Our results imply that the extended radio emission in Abell 2146 is probably associated with shocks and turbulence during cluster merger. The relativistic electrons in the NW and SE may originate from fossil plasma and thermal electrons, respectively.

5.1 Introduction

Extended radio synchrotron emission (∼ Mpc-scale) in clusters is generally associated with large-scale shocks and turbulence that are generated in the intra-cluster medium (ICM) during the formation of galaxy clusters (see, e.g., Ferrari et al. 2008; Feretti et al. 2012; Brunetti & Jones 2014 for reviews). The detection of this emission reveals the presence of relativistic particles (i.e. cosmic rays, CRs) and magnetic fields in the ICM. Based on its physical properties, the extended emission is commonly classified as either a relic or a halo (e.g. Kempner et al. 2004). Radio relics are elongated, highly polarized, steep spectrum sources that are usually observed at the cluster periphery. Radio haloes are roundly-shaped, apparently unpolarized sources that are found in the central regions of clusters. Due to the short cooling timescale of the radio-emitting relativistic electrons through synchrotron and inverse-Compton (IC) energy losses in ∼ μG magnetic fields, the ∼ Mpc scale of radio relics and haloes implies that CRs must be (re-)accelerated in situ (Jaffe 1977).

The favored mechanism of particle acceleration in haloes is where CRs are energized by turbulence during cluster mergers (e.g. Brunetti et al. 2001; Petrosian 2001; Fujita et al. 2003; Cassano & Brunetti 2005; Brunetti & Lazarian 2007, 2016; Pinzke et al. 2017). The collisions of the relativistic protons and thermal protons in the ICM (i.e. the hadronic model), that produce secondary relativistic electrons, may also contribute to the observed radio emission (e.g. Dennison 1980; Blasi & Colafrancesco 1999; Dolag & Ensslin 2000; Miniati et al. 2001; Pfrommer & Enßlin 2004; Pfrommer 2008; Keshet & Loeb 2010; Enßlin et al. 2011). However, pure hadronic models for radio haloes are severely challenged by limits from Fermi-LAT observations (e.g. Jeltema & Profumo 2011; Brunetti et al. 2012; Zandanel et al. 2014; Ackermann et al. 2010, 2016), although hadronic models in which secondary particles are re-accelerated by turbulence might be still possible to explain the radio emission in haloes (Brunetti & Lazarian 2011a; Brunetti et al. 2017; Pinzke et al. 2017). The generation and dissipation of turbulence in the ICM is a complicated process and involves a complex chain of mechanisms (see, e.g., Brunetti & Jones 2014 for review). For example, the gravitational potential induced by the motion of dark matter sub-haloes can cause a mixing of the gas and a stretching of the magnetic fields in the ICM generating instabilities at different scales (e.g. Cassano & Brunetti 2003; Fujita et al. 2004; ZuHone et al. 2013; Miniati 2014). Also merger shocks driven in the ICM can generate turbulence at different scales.
via baroclinic and compressive processes (e.g. Iapichino & Niemeyer 2008; Iapichino et al. 2008, 2011; Vazza et al. 2017).

The relativistic electrons in relics are thought to be more locally generated through Fermi-I acceleration by cluster-scale shocks during the collisions of sub-clusters/groups (e.g. Enßlin et al. 1998; Roettiger et al. 1999). The observation evidence for this is that radio relics have been observed at the location of some X-ray shock fronts (e.g. Shimwell et al. 2015; Botteon et al. 2016a; Eckert et al. 2016; Akamatsu et al. 2017; van Weeren et al. 2016c, 2017; Urdampilleta et al. 2018). The steepening of the radio spectral index across the width of the elongated relics provides additional evidence that relativistic electrons in relics are (re-)accelerated at shock fronts and lose their energy in the post-shock region due to synchrotron and IC energy losses (e.g. Giacintucci et al. 2008; van Weeren et al. 2010; Stroe et al. 2013; Hoang et al. 2017; Hindson et al. 2014). Moreover, the alignment of magnetic field vectors along the length of some relics implies a compression of the magnetic fields in these regions which is an expected consequence of a passing shock front (e.g. Bonafede et al. 2009, 2012; Kale et al. 2012; de Gasperin et al. 2014; Pearce et al. 2017; Hoang et al. 2018a).

Despite of the observational evidence associating radio relics with shocks, radio relics have not been firmly detected at all known strong ($M \approx 2 – 3$) cluster shocks. For example, relics are not obviously associated with shocks in Abell 520 (e.g. Markevitch et al. 2005; Govoni et al. 2001b; Vacca et al. 2014; Hoang et al. 2018a; submitted), the western edge of the Bullet cluster (1E065 – 558; e.g. Markevitch et al. 2002; Shimwell et al. 2014), Abell 665 (e.g. Feretti et al. 2004; Dasadia et al. 2016), and Abell 2146 (e.g. Russell et al. 2010; Hlavacek-Larrondo et al. 2018). In these regions, extended radio emission is either undetected at the shocks (e.g. Abell 665), the spectrum of the observed radio emission does not steepen in the post-shock region (e.g. the Bullet cluster) or the distribution of spectral index has not been obtained (e.g. Abell 2146). Moreover, polarimetric measurements have not been reported for most of these clusters, except for the Bullet cluster. The non-detection of radio relics at these shocks would challenge the shock-related formation model of radio relics, however observational limitations should be carefully sorted out. To address this problem, we have performed new low-frequency radio observations of galaxy clusters with prominent shocks but debated or no radio relic emission, i.e., Abell 520 (Hoang et al. 2018b), Abell 665, and Abell 2146 (Hoang et al. 2018c).
5.2 The galaxy cluster Abell 2146

Abell 2146 (hereafter A2146; $z = 0.232$) is a binary merging galaxy cluster where the first core passage occurred approximately 0.24-0.28 Gyr ago in the plane of the sky. (e.g. Russell et al. 2010, 2011, 2012; Rodríguez-González et al. 2011; Canning et al. 2012; White et al. 2015; King et al. 2016; Coleman et al. 2017; Hlavacek-Larrondo et al. 2018). The total mass of A2146 is estimated to be $M_{500} = (4.04 \pm 0.27) \times 10^{14} M_\odot$ (Planck Collaboration et al. 2016). Chandra X-ray observations revealed a NW-SE elongation and a highly disturbed morphology of the thermal ICM (Russell et al. 2010). Detailed analysis of the X-ray surface brightness (SB) and temperature distribution revealed a bow shock in the SE region and an upstream shock in the NW region (Russell et al. 2010, 2012). From the jumps in the X-ray derived density profiles, Russell et al. (2012) estimated Mach numbers of $M_{\text{SE}}^X = 2.3 \pm 0.2$ and $M_{\text{NW}}^X = 1.6 \pm 0.2$ for the SE and NW shocks, respectively. Despite A2146 being a highly disturbed cluster with clear shock fronts, initially radio observations did not detect extended radio emission from the cluster (Russell et al. 2011). However, recently Hlavacek-Larrondo et al. (2018) discovered radio emission extending up to $\sim 850$ kpc with deep VLA L-band observations. The ~30 arcsec-resolution VLA L-band image shows two separated patches of extended emission in the NW and SE regions. Based on the location and morphology, Hlavacek-Larrondo et al. (2018) suspect that the NW emission is a radio relic associated with the NW upstream shock. Although Hlavacek-Larrondo et al. (2018) suggested that the SE emission might be a radio halo, they also speculated whether or not it may consist of a halo and a relic which could not be separated with their low-resolution VLA image. However, for both the NW and SE regions key observational evidence to connect the extended radio emission (i.e. relics) with the shocks (i.e. spectral steepening in the post-shock regions and the alignment of magnetic fields at the shock fronts) is still missing. Thus, the precise nature of the diffuse radio emission in A2146 still needs to be determined.

In this paper, we present deep LOFAR 120 – 168 MHz observations of A2146. We aim to map the extended emission from A2146 at 144 MHz with a high resolution ($\lesssim 15$ arcsec). To study spectral properties of the radio emission from the cluster, we combine the LOFAR 144 MHz data with the existing VLA 1 – 2 GHz data presented in Hlavacek-Larrondo et al. (2018) and the archival GMRT 222 – 254 and 596 – 628 MHz data. We assume the cosmological parameters, $H_0 = 70$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_M = 0.3$, and $\Omega_A = 0.7$. 

5.3 Observations and data reduction

5.3.1 LOFAR 144 MHz

A2146 was observed for a total of 16 hours split over two dates (ObsID: L589831 and L6311955) with LOFAR (Haarlem et al. 2013). One of the observations (i.e. L589831) forms part of the LOFAR Two-meter Sky Survey (LoTSS; Shimwell et al. 2017) and has a pointing center of 1.3° from the target. The other is a targeted observation centered on A2146. A summary of the observations is given in Table 5.1.

We have calibrated the LOFAR data to correct for direction-independent and direction-dependent effects using the facet calibration technique described in van Weeren et al. (2016a) and Williams et al. (2016) and summarized here for completeness. The direction-independent calibration (see de Gasperin et al. (2018) for an overview of direction independent effects) is done using the Prefactor pipeline which includes flagging radio frequency interference (RFI), removing contamination from bright sources in the distant sidelobes (i.e. Cassiopeia A and Cygnus A), correcting the amplitude gain, the initial clock offsets and XX-YY phase offsets. The calibration parameters were derived from 10 min observations of the primary calibrators 3C 196 and 3C 295 (Obs. IDs: L589831 and L6311955). The 3C 196 and 3C 295 models used to calibrate these data have integrated flux densities which are consistent with the Scaife & Heald (2012) flux scale. After the target data are calibrated with the solutions derived from the calibrator observations, the data are phase calibrated against a wide-field sky model obtained from the TIFR GMRT 150 MHz All-sky Radio Survey: First Alternative Data Release (TGSS-ADR1; Intema et al. 2017). The direction-dependent calibration is performed separately on each dataset using the Factor pipeline which aims to correct for ionospheric distortions and errors in the primary beam model to allow for accurate calibration in the direction of A2146.

To obtain continuum images, the data calibrated in the direction of A2146 were deconvolved with MS – MFS (multiscale-multifrequency) with nterms = 2 and W-projection options in the Common Astronomy Software Applications package (CASA) to account for the frequency dependence

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1 https://github.com/lofar-astron/prefactor
2 https://github.com/lofar-astron/factor
<table>
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<th>Telescope</th>
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<th>GMR</th>
<th>T238 MHz</th>
<th>GMR</th>
<th>T612 MHz</th>
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<td>20_063, ICF7_024</td>
<td>DDT9_001, 20_063</td>
<td>ICF7_024, DDT9_001</td>
<td>20_063, 12D1_009</td>
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<td>144</td>
<td>144</td>
<td>144</td>
<td>144</td>
<td>144</td>
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<tr>
<td>Total on-source time (hr)</td>
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<td>15.1</td>
<td>11.1</td>
<td>16.7</td>
<td>15.1</td>
<td>11.1</td>
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<td>Observing dates</td>
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<td>Apr. 27, 2012 (B), May 9, 2012 (C), June 17, 2012 (D)</td>
<td>Apr. 27, 2012 (B), May 9, 2012 (C), June 17, 2012 (D)</td>
<td>Apr. 27, 2012 (B), May 9, 2012 (C), June 17, 2012 (D)</td>
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<td>58931, L631955, 369536</td>
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<td>XX, XY, YY, YX</td>
<td>XX, XY, YY, YX</td>
<td>XX, XY, YY, YX</td>
<td>XX, XY, YY, YX</td>
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<td>116, 163 (B), 5 (C, D)</td>
<td>116, 163 (B), 5 (C, D)</td>
<td>116, 163 (B), 5 (C, D)</td>
<td>116, 163 (B), 5 (C, D)</td>
<td>116, 163 (B), 5 (C, D)</td>
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<td>Number of antennas</td>
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Table 5.1: Observation details

Characterizing the radio emission from Abell 2146
5.3 Observations and data reduction

of the sky and non-coplanar effects (Cornwell et al. 2005, 2008; Rau & Cornwell 2011). To map emission at different scales, we make continuum images with various different weightings of the visibilities. All continuum images that were obtained from the observations were corrected for primary beam attenuations. To minimize the uncertainty in the LOFAR flux scale, the LOFAR images obtained from the observations L589831 and L6311955 are multiplied by factors of $1.02$ and $1.18$, respectively; where these scaling factors were obtained by comparing the integrated flux densities of nearby compact sources in the LOFAR images with those from the TGSS-ADR1 (Intema et al. 2017). The pixel values for the final combined continuum image are calculated as the average of the primary beam, corrected images, weighted by the local noise in each image.

5.3.2 GMRT 238 and 612 MHz

The GMRT 238 and 612 MHz observations of A2146 were carried out on Jun. 5, 2011 and Mar. 17, 2012 (Obs. IDs: 5369 and 5888). Table 5.1 provides more details on the observations. Each data set was separately calibrated using the Source Peeling and Atmospheric Modeling package (SPAM; Intema et al. 2009, 2017). This calibration mainly aims to correct for the ionospheric distortion which includes an interferometric phase delay. The amplitude gains were calibrated according to the flux scale in Scaife & Heald (2012). The flux scale error of 10% is used for the GMRT observations (e.g. Chandra et al. 2004). The final continuum images of A2146 at 612 MHz were obtained by averaging the primary beam corrected images from the different observations.

5.3.3 VLA 1.5 GHz

A2146 was observed for a total of 11.1 hours with the VLA at 1.5 GHz in B, C and D configurations on multiple dates in 2012 and 2013. The frequency bandwidth is divided into two intermediate frequency (IF) pairs, each of which has 8 sub-bands of 64 MHz. The observations were done with full-polarization settings. The integration time was set at 3 seconds for the B-configuration and 5 seconds for the C- and D-configurations. More details on the VLA observations are given in Table 5.1.

The calibration for each configuration of the VLA datasets was done separately in CASA by Hlavacek-Larrondo et al. (2018). For a full description of the procedure, we refer to Hlavacek-Larrondo et al. (2018). To obtain continuum images, the calibrated data of the B-, C- and D-configurations
were combined and imaged with the MS–MFS and W–projection algorithms in CASA.

5.3.4 Spectral measurements

We make a spectral index map to study the spectral energy distribution of the extended emission from A2146. The spectral index map is made with the LOFAR 144 MHz and VLA 1.5 GHz data. The LOFAR and VLA continuum images used for the spectral index mapping are imaged with the same parameters (i.e. uv-range of 0.12 – 65 kλ, Briggs’ robust weighting of 0.0, outertaper of 15 arcsec and 30 arcsec for the LOFAR and VLA, respectively, to obtain an approximate resolution of 30 arcsec). The spectral index $\alpha$ and the corresponding error for each pixel are estimated as

$$\alpha = \frac{\ln S_1}{\ln \frac{v_1}{v_2}} \quad \text{and} \quad \Delta \alpha = \frac{1}{\ln \frac{v_1}{v_2}} \sqrt{\left(\frac{\Delta S_1}{S_1}\right)^2 + \left(\frac{\Delta S_2}{S_2}\right)^2},$$

where $\Delta S_i = \sqrt{(\sigma_i)^2 + (f_{\text{err}} S_i)^2}$ with $i = [1, 2]$ is the total error associating with the flux density measurement $S_i$; and the subscripts 1 and 2 stand for 144 MHz and 1.5 GHz, respectively. The total error is propagated from the flux scale uncertainty (i.e. $f_{\text{err}} = 15\%$ and $5\%$ are commonly used for the LOFAR and VLA observations, respectively) and the image noise ($\sigma$).

5.4 Results and discussion

In Fig. 5.1, we present LOFAR 144 MHz continuum images of A2146. In this section, we estimate flux densities and spectral index for the compact and extended sources in the cluster and discuss the implications.

5.4.1 The radio galaxies

A2146 is known to host two bright radio galaxies (namely A2146-A and A2146-B) that are located in the central regions of the NW and SW sub-clusters (see Fig. 5.1, left). One of these is the brightest cluster galaxy (BCG) belonging to the SE sub-cluster (e.g. Russell et al. 2011). In projection, the radio galaxies are approximately coincident with the extended non-thermal emission from the ICM (Hlavacek-Larrondo et al. 2018) and are situated behind the SE and NW merger shocks (e.g. Russell et al. 2011).
5.4 Results and discussion

Figure 5.1: HST composite optical (left) and Chandra (right) images overlaid with the LOFAR 144 MHz contours (blue in the right panel). The resolutions of the LOFAR contours shown in the bottom-left corner are 14 arcsec $\times$ 11 arcsec ($P.A. = 55^\circ$, left) and 15 arcsec $\times$ 15 arcsec (right). In the right panel, the compact radio sources marked with the cyan circles are subtracted in the uv-data. The magenta dashed lines show the shock locations. In both images, the LOFAR contours start from $\pm 2.5\sigma$ (dotted negative), where $\sigma = 135$ and 160 $\mu$Jy beam$^{-1}$ in the left and right panels, respectively. The Chandra first contour is $2 \times 10^{-9}$ cts cm$^{-2}$s$^{-1}$arcsec$^{-2}$. The next contours are spaced by a factor of $\sqrt{3}$.

Figure 5.2: The spectral energy distribution between 144 MHz and 5 GHz for A2146-A and A2146-B. The flux densities are summarized in Table 5.2.
Characterizing the radio emission from Abell 2146

Table 5.2: Flux density for the radio galaxies in the vicinity of A2146.

<table>
<thead>
<tr>
<th>Freq. (MHz)</th>
<th>$S_{A2146-A}$ (mJy)</th>
<th>$S_{A2146-B}$ (mJy)</th>
<th>Telescope</th>
<th>Ref.</th>
</tr>
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<tr>
<td>144</td>
<td>75 ± 11</td>
<td>166 ± 25</td>
<td>LOFAR</td>
<td>this paper</td>
</tr>
<tr>
<td>150</td>
<td>-</td>
<td>183 ± 21</td>
<td>GMRT</td>
<td>a</td>
</tr>
<tr>
<td>238</td>
<td>56.8 ± 5.7</td>
<td>106.1 ± 10.6</td>
<td>GMRT</td>
<td>this paper</td>
</tr>
<tr>
<td>325</td>
<td>47 ± 5</td>
<td>93 ± 9</td>
<td>GMRT</td>
<td>b</td>
</tr>
<tr>
<td>612</td>
<td>37.8 ± 3.8</td>
<td>67.6 ± 6.8</td>
<td>GMRT</td>
<td>this paper</td>
</tr>
<tr>
<td>1400</td>
<td>15.6 ± 3.5</td>
<td>36.6 ± 4.0</td>
<td>VLA</td>
<td>a</td>
</tr>
<tr>
<td>5000</td>
<td>6.6 ± 0.3</td>
<td>8.9 ± 0.5</td>
<td>VLA</td>
<td>c, a</td>
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</table>


The total flux density of these sources at 144 MHz is 75±11 mJy for A2146-A (i.e. the SE BCG) and 166±25 mJy for A2146-B. We also obtained measurements at 150 MHz from the TGSS-ADR1 (Intema et al. 2017), 325 MHz (Russell et al. 2011), 612 MHz (see Sec. 5.3.2), VLA 1.5 GHz (Hlavacek-Larrondo et al. 2018) and 5 GHz (Hogan et al. 2015; Hlavacek-Larrondo et al. 2018) observations and present the spectral properties of these sources in Fig. 5.2 and Table 5.2. Since both A2146-A and A2146-B are present in the TGSS-ADR1 150 MHz image, but A2146-A resides in the region that has high background and is only detected at $\lesssim 2\sigma$, we exclude the TGSS-ADR1 flux density measurements for A2146-A in this analysis.

To estimate the integrated spectral indices for A2146-A and A2146-B, we fit their spectra with an exponential function, $S \propto \nu^\alpha$. In the fitting, the flux densities are weighted by the inverse square of the flux density errors. We find that the average spectral index is $-0.71 \pm 0.02$ for A2146-A and $-0.84 \pm 0.02$ for A2146-B. However, the spectral energy distribution in Fig. 5.2 hints at possible spectral breaks at about 612 MHz and 1.5 GHz for A2146-A and A2146-B, respectively. To quantify this, we fit the radio flux density of the galaxies with a double-power-law function. The resulting spectral indices are $\alpha_{144\text{MHz}}^{612\text{MHz}} = -0.53 \pm 0.11$ and $\alpha_{612\text{MHz}}^{5\text{GHz}} = -0.79 \pm 0.05$ for A2146-A and $\alpha_{144\text{MHz}}^{1.5\text{GHz}} = -0.64 \pm 0.06$ and $\alpha_{1.5\text{GHz}}^{5\text{GHz}} = -1.17 \pm 0.10$ for A2146-B where in both cases the spectral index steepens at high frequencies. The spectral steepening of A2146-A and A2146-B at high frequencies might be due to the synchrotron and IC energy losses of the radio emitting particles.

It is noted that the spectrum below 612 MHz for A2146-A roughly follows a single power law function, $S \propto \nu^\alpha$, and does not indicate a sharp
5.4 Results and discussion

turnover at low frequencies as reported in Hlavacek-Larrondo et al. (2018) which used GMRT 150 MHz data.

5.4.2 The NW extended emission

In Fig. 5.1, the NW radio emission extends over a region of $200 \times 310$ kpc$^2$. The NW radio emission is elongated in the NE-SW direction which is approximately perpendicular to the merger axis (e.g. White et al. 2015). The outer edge of the NW radio emission is located behind the detected upstream X-ray shock (Russell et al. 2010). The integrated flux densities of the NW emission measured within the $2.5\sigma$ contours are $S_{144 \text{ MHz}} = 13.1 \pm 2.0$ mJy and $S_{1.5 \text{ GHz}} = 0.89 \pm 0.08$ mJy, resulting in an integrated spectral index of $\alpha = -1.14 \pm 0.08$. This spectral index measurement for the NW radio emission is typical value for an elongated relic known (i.e. $\alpha \approx -1.3$; Feretti et al. 2012). However, our spectral index is flatter than the 1-2 GHz in-band measurement of $\alpha_{1-2 \text{ GHz}} = -2.3 \pm 0.3$ that was reported in Hlavacek-Larrondo et al. (2018). As mentioned by Hlavacek-Larrondo et al. (2018), the true uncertainty of the in-band spectral measurement is likely higher. However, if the true value of the 1-2 GHz spectral index of the NW emission is indeed this steep then it would imply a spectral curvature between 144 MHz and 1.5 GHz. Unfortunately, we are unable to check this possibility because the NW extended emission has only been detected at 144 MHz and 1.5 GHz.

To examine the distribution of the spectral index and search for a spectral index gradient that is often associated with radio relics, we make the spectral index map in Fig. 5.3 and the spectral index profile in Fig. 5.4. In the spectral index profile a steepening of the spectral index of the NW emission approximately along the merger axis is apparent. In the outer region, the spectral index is $-1.06 \pm 0.06$, but steepens to $-1.29 \pm 0.09$ in the inner region about 170 kpc from the outer 2.5$\sigma$ contour. Since we examine the spectral trend, the flux scale errors due to the amplitude calibration are not used in the calculation of the spectral index errors. We emphasize that due to the limited resolution of our spectral index map we are only able to make two independent measurements of the spectral index in the region of NW emission and that it is important to confirm the spectral gradient across the NW extended radio emission with high-resolution observations.

Basing on the morphology of the NW radio emission, Hlavacek-Larrondo et al. (2018) concluded that it is likely a radio relic. A number of radio relics have been observed to have steeper spectra toward the cluster center (e.g. Bonafede et al. 2009; Kale et al. 2012; de Gasperin et al. 2015; van
Figure 5.3: The 30 arcsec-resolution spectral index (left) and error (right) maps between 144 MHz – 1.5 GHz for the extended radio emission from A2146. In both images, the LOFAR 144 MHz (blue) and VLA 1.5 GHz (gray) first contours are 2.5σ, where σ = 340 and 27 μJy beam⁻¹ for the LOFAR 144 MHz and VLA 1.5 GHz data, respectively. The next contours are multiplied by \sqrt{3}.

Figure 5.4: The SB (top) and spectral index (bottom) profiles for the extended radio emission from A2146. The flux scale errors are not added to the total errors of the flux densities. The numbers next to the data points indicate the region numbers shown in overlaid image. The red circular regions at the locations of the subtracted compact sources are masked.
The spectral steepening is due to the energy losses through the synchrotron and IC emission. In the spectral analysis above, we show that the radio spectral index in the region behind the NW shock front is steeper than that in the outer edge, which supports the nature of the NW extended radio emission being a radio relic. Its location and spectral properties imply that the NW extended emission is likely to be associated with the NW upstream shock. Shocks will compress ICM magnetic fields resulting in polarized radio emission. Therefore, new radio polarization observations will provide further information on the relation between the shock and extended emission in the NW region of the cluster.

According to the diffusive shock acceleration (DSA) (e.g. Blandford & Eichler 1987), a shock of Mach number $M$ should accelerate thermal electrons and generate a population of relativistic electrons with an energy spectrum,

$$\frac{dN}{dy} = N_0 \gamma^{-\delta_{inj}},$$

(5.2)

where $N_0$ and $\gamma$ are the spectral normalization and Lorentz factors, respectively; the spectral slope $\delta_{inj}$ is related to the shock Mach number via

$$\delta_{inj} = 2 \frac{M^2 + 1}{M^2 - 1}.$$  

(5.3)

In the presence of magnetic fields, the relativistic electrons emit synchrotron radiation with a spectrum of $I \propto \nu^{\alpha_{inj}}$, where $\alpha_{inj} = (1 - \delta_{inj})/2$. The NW upstream shock in A2146 has a Mach number of $M = 1.6 \pm 0.1$ that was derived from the X-ray SB jump (Russell et al. 2012). According to the DSA model, we should therefore observe radio emission along the shock with an injection spectral index of $\alpha_{inj} = -1.78^{+0.22}_{-0.32}$. This prediction is steeper than our estimate (i.e. $\alpha_{inj} = -1.06 \pm 0.09$ which takes into account the flux scale errors of 15% and 5% for LOFAR and VLA, respectively). The discrepancy should not be caused by the resolution of the radio observations because if there is indeed a spectral index gradient then at higher resolution the index would be even flatter in the region closer to the shock front. The discrepancy could be because the shock is not powerful enough to efficiently accelerate thermal electrons and is instead (re-)accelerating pre-existing fossil electrons. Such electrons could be remnants of lobes of radio galaxies (e.g. Markevitch et al. 2005; Kang et al. 2012). In this scenario, the shock increases the brightness of the radio emission, but preserves the spectrum of the pre-shock fossil electrons if the fossil electrons have flatter spectrum than that generated by the shock (e.g. Markevitch et al. 2005). If fossil
electrons were being re-accelerated we may see extended radio emission in front of the shock (Markevitch et al. 2005) but this is not present in the LOFAR 144 MHz and VLA 1.5 GHz observations (Figs. 5.1 and 5.3). Finally, we do note that the spectral index of $-1.06$ that we estimated for the NW outer region is the typical value for the lobes of radio galaxies although unlike van Weeren et al. (2017) the potential source of the fossil electrons in the NW region of the cluster is not obvious.

As discussed in van Weeren et al. (2016c) for the Toothbrush relic, an alternative explanation for the mismatch of injection indices obtained from the radio observations and the DSA model is that the shock might contain different Mach numbers along the line of sight (e.g. Skillman et al. 2011, 2013; Vazza et al. 2012). In the case of a nonlinear dependence of the Mach numbers on the acceleration efficiency (e.g. Hoeft et al. 2007), the radio observations are particularly sensitive to the shocks with high Mach numbers (resulting in flat spectrum radio emission), while the X-ray observations tend to observe the lower Mach number shocks (corresponding to steep spectrum radio emission). This explanation is supported by recent simulations of particle acceleration at cluster merger shocks in Hong et al. (2015) and Ha et al. (2018). These studies reported that the weighted Mach numbers derived from the gas temperature jumps are smaller than those obtained from the shock kinetic energy flux (i.e. radio data). Hence, the discrepancy between the injection indices derived from spectral index map and the DSA model might be explained if the shock consists of multiple Mach numbers along the line of sight. We note that if we use the Mach number $M_{NW} = 2.0 \pm 0.3$ calculated from temperature jump (Russell et al. 2012), the injection index predicted by the DSA model is $\alpha = -1.17^{+0.20}_{-0.39}$ which is consistent with our injection spectral measurement (i.e. $\alpha_{\text{inj}} = -1.06 \pm 0.09$). However, Russell et al. (2012) pointed out that the Mach number calculated from the temperature jump is less accurate due to the large radial bins which cannot resolve the shock jump accurately.

The Mach numbers calculated from X-ray SB density jump could be biased low due to projection effects. Without the correction for the projection effects, this bias increases the difference between the X-ray and radio derived Mach numbers (or the DSA predicted and observed injection indices). However, as two sub-clusters in A2146 are known to merge almost on the plane of the sky (i.e. the angle between the merger axis and the plane of the sky is $\sim 16^\circ$; White et al. 2015), the viewing angle to the NW shock is likely to be edge on. Hence, the projection effects might not play an important role in the mismatching of the DSA predicted and radio observed injection
5.4 Results and discussion

Figure 5.5: Regions (dashed lines) where flux densities were extracted are shown on the LOFAR 144 MHz 30 arcsec-resolution image. The LOFAR 144 MHz (blue) and VLA 1.5 GHz (gray) contours are identical to those in Fig. 5.3.

indices in the NW extended emission.

5.4.3 The radio bridge

In Fig. 5.1, the NW relic is connected with the SE extended emission through a faint emission (bridge). We measure the flux density of the radio emission in the bridge using the $> 2.5\sigma$ pixels within the region of the bridge (see Fig. 5.5). The integrated flux density of the emission in the bridge is 1.1 mJy at 144 MHz, but it is undetected at 1.5 GHz (see Figs. 5.3 and 5.5). We assume the size of the bridge emission at 1.5 GHz is similar to that at 144 MHz. We find that 1σ upper limit for the bridge emission at 1.5 GHz is 0.047 mJy. This implies that the integrated spectral index of the emission in the bridge is likely steeper than $-1.3$. The elongated morphology of the bridge along the merger axis implies that it likely associates with the turbulence induced by the on-going merger. However, it is still unclear whether or not the bridge emission is a separated source or is part of the SE extended emission.
5.4.4 The SE extended emission

In Fig. 5.1, we show the SE extended emission at 144 MHz. The SE emission has a projected size of $300 \times 350\text{kpc}^2$ and is elongated in the NW-SE direction. The SE edge of the SE emission roughly follows the SE bow shock (e.g. Russell et al. 2010). The integrated flux density of the SE extended emission (without the bridge, see Figs. 5.1 and 5.5) encompassing $2.5\sigma$ contours is $24.3 \pm 3.8\text{ mJy}$ at 144 MHz and $1.3 \pm 0.1\text{ mJy}$ at 1.5 GHz. The spectral index between 144 MHz and 1.5 GHz is $\alpha = -1.25 \pm 0.07$. Unlike the spectral index estimate for the NW relic, our spectral index measurement for the SE emission is consistent with the VLA in-band estimate of $-1.2 \pm 0.1$ that was presented in Hlavacek-Larrondo et al. (2018). The spectral index map in Fig. 5.3 shows a patchy distribution in the SE region. Along the SE-NW merger axis, the SE extended emission has a flat spectrum in the SE region and the spectrum becomes steeper toward the NW direction. The trend is more visible in the spectral index profile in Fig. 5.4.

The nature of the SE extended emission is still unclear. Possibilities include: (i) a radio halo bounded by a merger shock (e.g. Markevitch et al. 2005; Shimwell et al. 2014; Markevitch 2010; Brown & Rudnick 2011; van Weeren et al. 2016c); (ii) a radio relic on the SE edge superimposed on a radio halo that extends outwards from the cluster center (e.g. Brunetti et al. 2008; Macario et al. 2011; van Weeren et al. 2016c; Hoang et al. 2017). Scenario (ii) was the favored scenario in Hlavacek-Larrondo et al. (2018). The extended emission in scenarios (i) and (ii) can perhaps be generated by the same merger; but the distinct appearance of the radio emission and its spectrum depends on the shock Mach number, the magnetic field strength behind the shock front, the spectral energy distribution of turbulence after the shock passage, and the observing frequencies (Markevitch 2010). It is noted that the SE edge of the SE extended emission is not spatially coincident with the entire shock front (see Fig. 5.1, right), although the location and orientation of the SE extended emission along the merger axis seems to imply its shock-related origin.

According to scenario (ii) the SE extended emission (Fig 5.1) should consist of two components. To assess this we make surface brightness profiles along the merger axis in Fig. 5.4. To take into account the size of the synthesis beam, each data point is estimated in a region that encompasses a beam (15 arcsec or 30 arcsec). The brightness peaks in the SE extended radio emission are clearest in the 15 arcsec-resolution profile as in the 30 arcsec-resolution profile they are smoothed out. We note that the extended emission maps are obtained by subtracting compact sources (i.e.
cyan circles in Fig. 5.1, right) which will leave some residual flux which contaminates the profiles. However, if there are two separate sources (i.e. halo and relic) in the SE region, the width of the relic can be approximated as the distance from the SE $2.5\sigma$ contour to the local minimum brightness in the 15 arcsec profile, which is about 170 kpc (Fig. 5.4). With this approximation we are able to estimate the halo flux, where estimates here should be considered as the lower limits for the halo flux density. To have consistent flux measurements at both frequencies, we measure the halo flux densities at 144 MHz and 1.5 GHz using the 30 arcsec images within the regions shown in Fig. 5.5. Only pixels that are detected at $> 2.5\sigma$, where $\sigma = 340$ and 27 $\mu$Jy beam$^{-1}$ for the LOFAR 144 MHz and VLA 1.5 GHz images, respectively, are used in the calculation. The integrated flux densities at 144 MHz for the relic and halo regions are 9.0 and 15.3 mJy, respectively. At 1.5 GHz, they are 0.53 and 0.78 mJy, respectively. With these measurements, we find the integrated spectral index to be $-1.2$ for the tentative relic and $-1.3$ for the halo. Since the separation of the relic and halo will need verification with high-resolution observations, the flux density estimated here should be considered as a rough estimate. The true value for the flux density of the halo at 144 MHz should lie in between 15.3 mJy (i.e. the SE extended emission consists of a relic and a halo) and 24.3 mJy (i.e. the SE extended emission is a single halo). At 1.5 GHz, it is between 0.78 mJy and 1.31 mJy. If the bridge emission is part of the SE extended emission, the upper limit for the flux density of the halo is 25.4 mJy at 144 MHz and 1.38 mJy at 1.5 GHz. The 1.4 GHz power for radio haloes, which is proportional to the amount of turbulence energy that is converted into the relativistic electrons, is known to correlate with the masses of their host clusters (e.g. Cassano et al. 2013). Using the flux density estimates above for the radio halo, we calculate the power of the A2146 halo at 1.4 GHz is within a range of $(1.5 - 2.5) \times 10^{23}$ W Hz$^{-1}$ (k-corrected). The power of the A2146 halo is consistent with the $P-M$ scaling relation with a cluster mass of $M_{500} = (4.04 \pm 0.27) \times 10^{14}$ M$_{\odot}$ (Planck Collaboration et al. 2016) that we present in Fig. 5.6.

Another key observational feature to distinguish whether the extended emission is a single halo (i.e. the case i) or a composition of a halo and a relic (i.e. the case ii) is the distribution of the spectral index of the radio emission along the axis of shock propagation. In case (ii), we expect the spectral index of the radio emission is flat immediately behind the shock front (i.e. due to shock (re-)acceleration or compression), steepening further in the post-shock region (i.e. because of synchrotron and IC losses) and might flatten
Figure 5.6: The $P - M$ correlation. The estimated range for the power of the radio halo in A2146 (red points) is roughly consistent with the $P - M$ scaling relation (i.e. black line). The gray shadow is the 95% confidence region. The downward arrows show upper limits for undetected haloes. For the list of the haloes in the plot, we refer to Cassano et al. (2013).

again in the halo region depending on the amount of turbulent energy induced by the passage of a merger shock available in the ICM. On the other hand, in case (i) whether or not we might see a similar spectral trend across the extended source behind the shock, depending on the physical conditions at the post-shock region. The spectral index of the halo emission might slightly steepen behind the shock and then become uniform across the halo region. These scenarios (i) and (ii) have been recently used to explain the spatial distribution of the spectral index in some clusters. Examples for the case (i) are the SW radio edge in Abell 520 (Hoang et al. 2018b, submitted) and, perhaps, the southern region of the radio halo in the Toothbrush cluster (van Weeren et al. 2016c; Rajpurohit et al. 2018). For case (ii), examples are the northern relics and the haloes in the Toothbrush and Sausage clusters (e.g. van Weeren et al. 2016c; Hoang et al. 2017). Whilst our spectral index maps are too low resolution to make firm conclusions, in the SE extended emission of A2146, there might be a spectral gradient from $-1.13 \pm 0.06$ to $-1.25 \pm 0.06$ behind the shock. This tentative trend is in line with that expected for a relic-halo superposition. If the SE extended radio emission is shock (re-)accelerated, the radio spectral index of $-1.13 \pm 0.06$ in the SE edge implies a shock Mach number of $M_{SE} = 2.0 \pm 0.1$. This is in line the
value estimated from the X-ray data (i.e. $M^{\text{X}}_{\text{SE}} = 2.3 \pm 0.2$; Russell et al. 2012), which makes the argument for a connection between the bow shock and the SE edge of the extended radio emission (i.e. the relic) in the SE region of the cluster more compelling.

5.5 Conclusions

In this paper, we present the results of deep LOFAR 120–168 MHz observations of the binary merging galaxy cluster A2146. We map the extended continuum emission at 144 MHz and the spectral energy distribution in the cluster in more detail than in previous studies. We summarize the results below.

- The LOFAR 144 MHz observations confirm the presence of the NW extended emission that was detected with the deep VLA 1.5 GHz observations (Hlavacek-Larrondo et al. 2018). The radio emission extends behind the upstream shock front and have a flux density of $13.1 \pm 2.0$ mJy at 144 MHz and $0.89 \pm 0.08$ mJy at 1.5 GHz. The integrated spectral index is $\alpha = -1.14 \pm 0.08$. The spectral index flattens to $-1.06 \pm 0.06$ in the outer region and steepens to $-1.29 \pm 0.09$ in the inner region. The morphological and spectral properties of the NW extended emission are consistent with the hypothesis that the NW extended emission is a relic associated with the NW upstream merger shock.

- The DSA model predicts an injection spectral index of $-1.78^{+0.22}_{-0.32}$ for the $M_{\text{NW}} = 1.6 \pm 0.1$ NW shock. However, we measure a spectral index in the outer region of the NW relic to be $-1.06 \pm 0.09$ (taken into account flux scale errors), which is inconsistent with the DSA prediction. The mismatching of the injection spectrum indices could be explained if the shock re-accelerates a pre-existing population of fossil electrons rather than those in the thermal pool.

- With the LOFAR 144 MHz observations, we detect a faint emission (bridge) connecting the NW and SE regions. The integrated flux density of the radio emission in the bridge is $1.1$ mJy at 144 MHz. The non-detection of the bridge with the VLA 1.5 GHz observations implies that the spectral index of the bridge emission is steeper than $-1.3$. 
The SE extended emission has an integrated flux density of \(24.3 \pm 3.8\) mJy at 144 MHz and \(1.3 \pm 0.1\) mJy at 1.5 GHz, resulting in \(\alpha = -1.25 \pm 0.07\). Further analysis of the brightness suggests that the SE extended emission may consist of a halo in the central region and a relic in the SE edge. The power for the radio halo is constrained within \((1.5-2.5) \times 10^{23}\) W Hz\(^{-1}\), which is roughly consistent with the expected power for the cluster mass (i.e. \(M_{500} = (4.04 \pm 0.27) \times 10^{14}\) M\(_{\odot}\); Planck Collaboration et al. 2016), according to the \(P - M\) scaling relation (Cassano et al. 2013).

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