

Cover Page



Universiteit Leiden



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KNOTS IN PLASMA

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The cover shows several magnetic surfaces of the self-organizing knotted magnetic equilibrium configuration identified in this research. The white surface is a (3, 2) magnetic island.

The image can be seen in 3d by crossing the eyes until the left and right image overlap, and relaxing the pupils to focus. This requires some practice.

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An electronic version of this dissertation is available at the Leiden University Repository (<https://openaccess.leidenuniv.nl>).

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for Science!

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