

A Stochastic quasi Newton method for molecular simulations

Chun Dong Chau

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Keywords: Stochastic Optimisation; Fokker Planck Equation; Quasi Newton; Langevin Dynamics; Limited Memory method.

Typeset in L^AT_EX.

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PROEFSCHRIFT

ter verkrijging van
de graad van Doctor aan de Universiteit Leiden,
op gezag van Rector Magnificus prof. mr. P. F. van der Heijden,
volgens besluit van het College voor Promoties
te verdedigen op woensdag 3 november 2010
klokke 15.00 uur

door

Chun Dong Chau

wiskundig ingenieur
geboren te Vlaardingen

in 1980

Promotiecommissie

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"Two things are infinite: the universe and human stupidity;
and I'm not sure about the the universe."

Albert Einstein



*To my family and the ones qualifying as family
because of our common denominator*

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